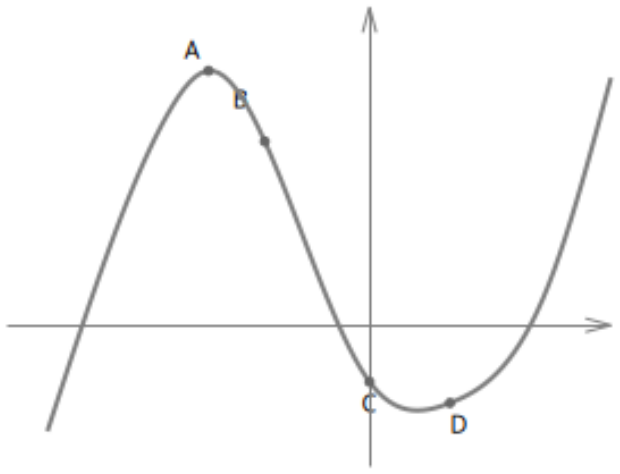
2.3 Concavity and the Second Derivative Worksheet

This document was composed and formatted by Annie Bernatchez.

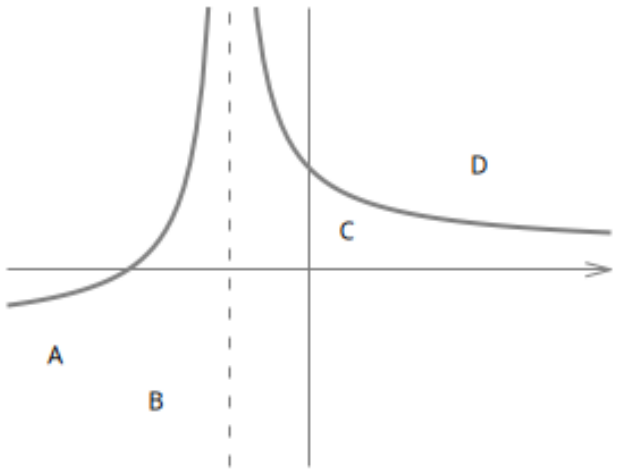
The course material originated from www.jensenmath.ca

1) For each function, state whether the value of the second derivative is positive or negative at each of points A, B, C, and D.

a)

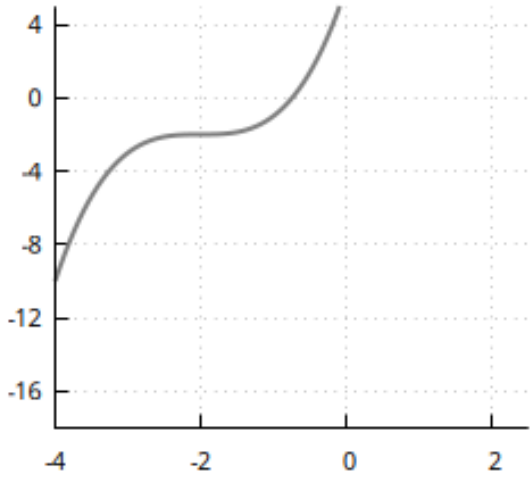


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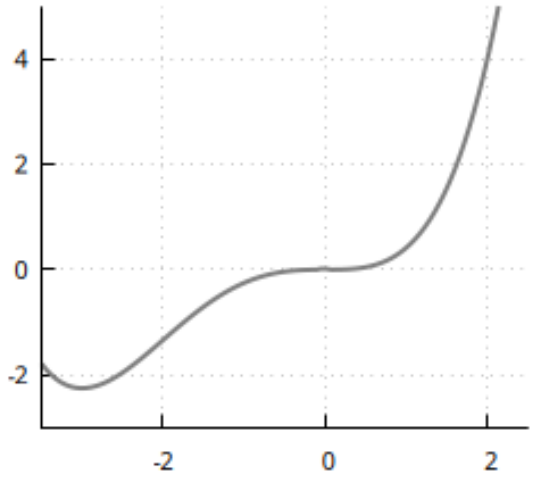


2) For each graph, identify the intervals over which the graph is concave up and the intervals over which it is concave down.

a)



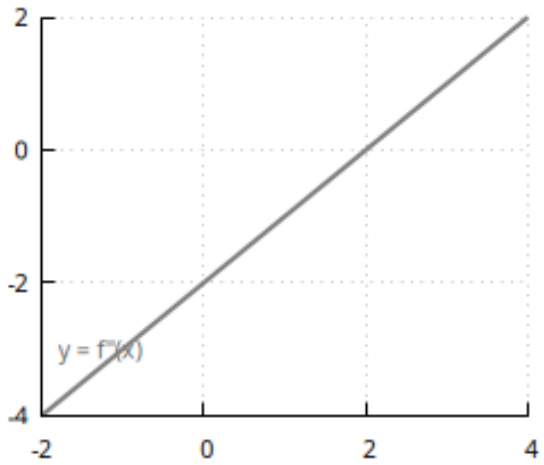
b)



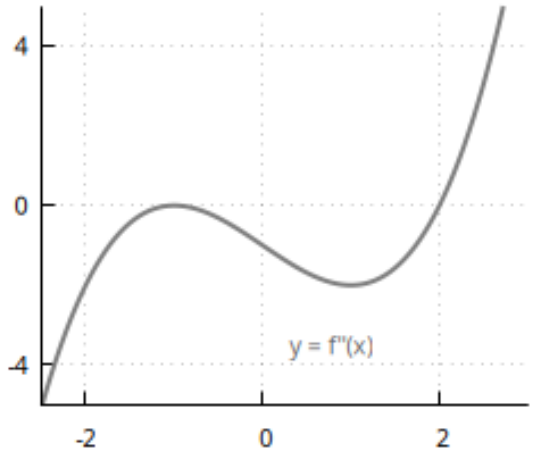
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3) Given each graph of $f''(x)$, state the intervals of concavity for the function $f(x)$. Also indicate where any points of inflection occur for $f(x)$.

a)



b)



4) For each function, find the intervals of concavity and the coordinates of any points of inflection.

a) $y = 6x^2 - 7x + 5$

b) $g(x) = -2x^3 + 12x^2 - 9$

Test		
$f''(x)$		
$f(x)$		

5) For each function, find and classify all the critical points using the second derivative test.

a) $y = x^2 + 10x - 11$

b) $f(x) = x^4 - 6x^2 + 10$

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6) Sketch a graph of a function that satisfies each set of conditions

a) $f''(x) = 2$ for all x, $f'(2) = 0$, $f(2) = -3$

b) $f''(x) > 0$ when $x < -1$, $f''(x) < 0$ when $x > -1$, $f'(-1) = 1$, $f(-1) = 2$

c) $f''(x) < 0$ when $-2 < x < 1$, $f''(x) > 0$ when $x < -2$ and $x > 1$, $f(-2) = -3$, $f(0) = 0$

Answer Key

1) a) A-neg, B-neg, C-pos, D-pos b) A-neg, B-neg, C-pos, D-neg

2) a) concave up: $x > -2$; concave down: $x < -2$ b) concave up: $x < -2$, $x > 0$; concave down: $-2 < x < 0$

3) a) concave up: $x > 2$; concave down: $x < 2$; POI when $x = 2$ b) concave up: $x > 2$; concave down: $x < -1$ and $-1 < x < 2$; POI when $x = 2$

4) a) always concave up b) concave up: $x < 2$; concave down: $x > 2$; POI at $(2, 23)$.

5) a) $(-5, -36)$ is a local min point b) $(-\sqrt{3}, 1)$ and $(\sqrt{3}, 1)$ are local mins, $(0, 10)$ is a local max

6) See figures above.

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