

4.2 Trig Ratios and Special Angles Lesson

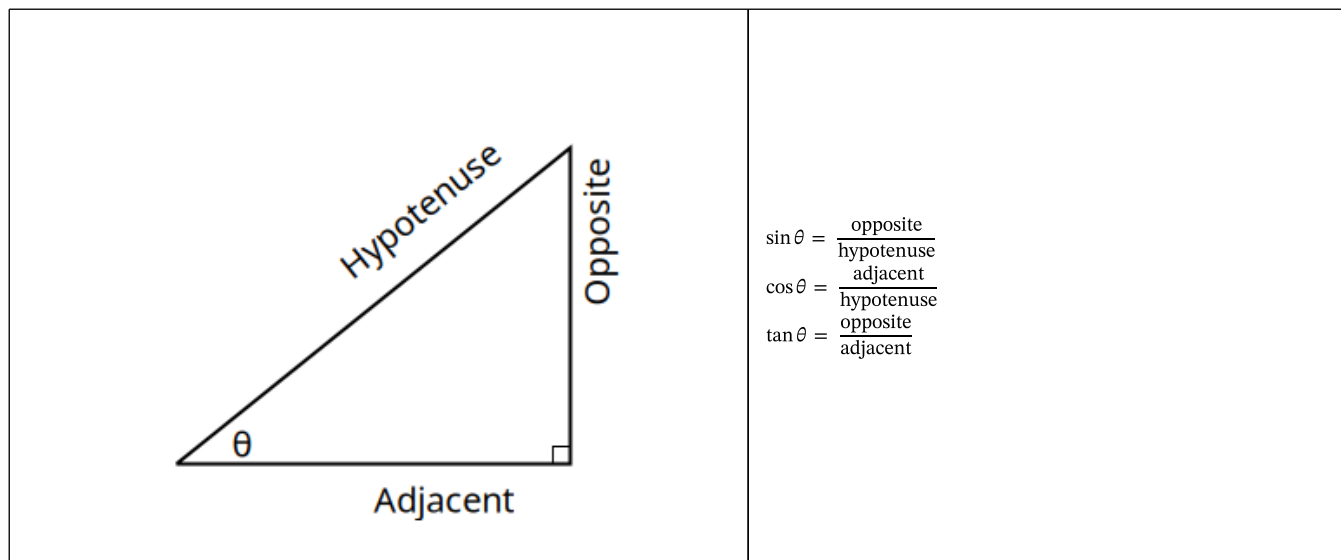
This document was composed and formatted by Annie Bernatchez.

The course material originated from www.jensenmath.ca

Part 1: Review of Last Year Trig

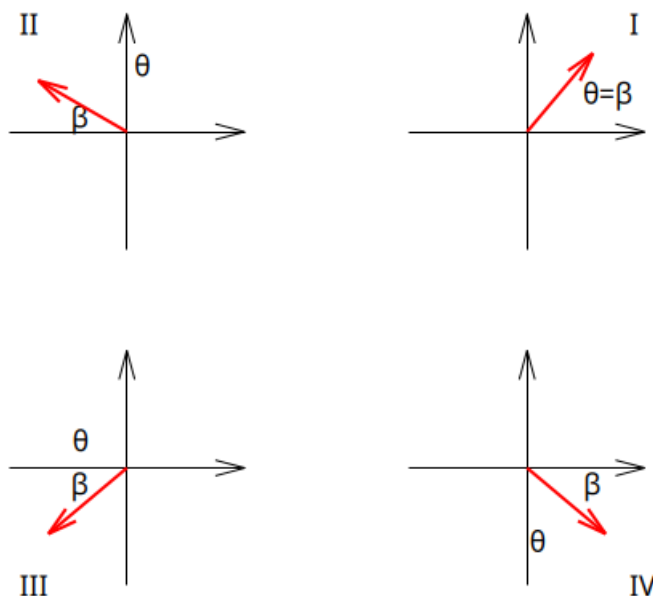
What is SOHCAHTOA?

If we know a right angle triangle has an angle of θ , all other right angle triangles with an angle of θ are _____ and therefore have equivalent ratios of corresponding sides. The three primary ratios are shown in the diagram to the right.



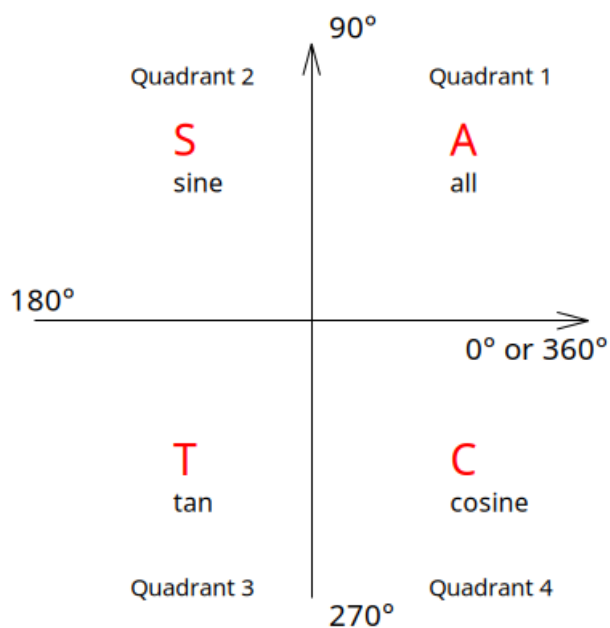
What is a reference angle?

Any angle over 90 has a reference angle. The reference angle is between 0° and 90° and helps us determine the exact trig ratios when we are given an obtuse angle (angle over 90 degrees). The reference angle is the angle between the terminal arm and the _____ ($0/360$ or 180).



What is the CAST rule?

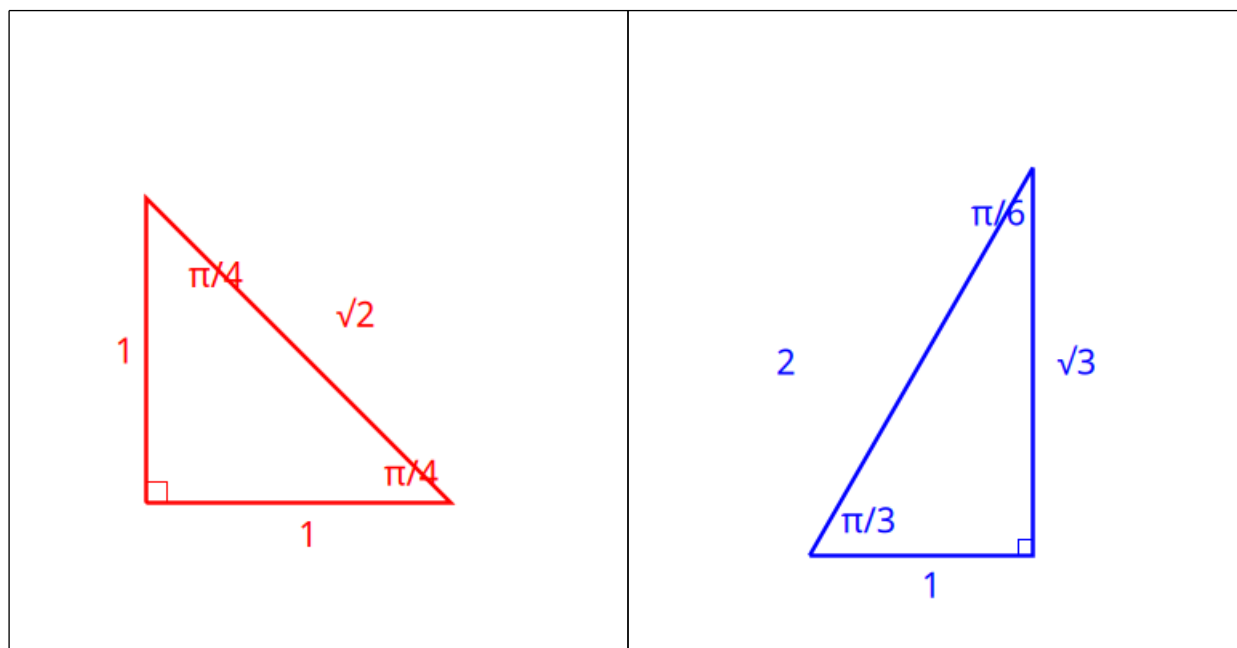
When finding the trig ratios of positive angles, we are rotating counter clockwise from 0 degrees toward 360. The CAST rule helps us determine which trig ratios _____ in each quadrant



Note: There are multiple angles that have the same trig ratio. You can use reference angles and the cast rule to find them.

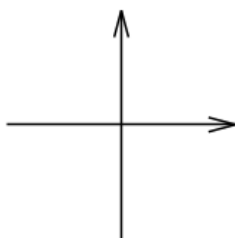
Part 2: Finding Exact Trig Ratios for Special Angles

Start by drawing both special triangles using radian measures

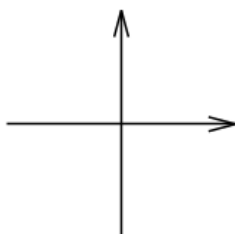


Example 1: Find the exact value for each given trig ratio.

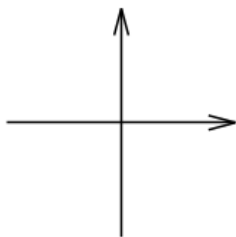
a) $\tan \frac{11\pi}{6}$



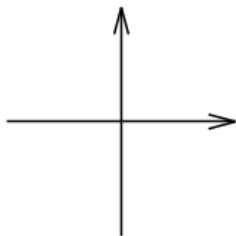
b) $\sin \frac{5\pi}{6}$



c) $\cos \frac{5\pi}{4}$



d) $\sec \frac{3\pi}{4}$



Example 2: Find the value of all 6 trig ratios for $\frac{5\pi}{3}$

Part 3: Application Question

Example 3: Justin is flying a kite at the end of a 50-m string. The sun is directly overhead, and the string makes an angle of $\frac{\pi}{6}$ with the ground. The wind speed increases, and the kite flies higher until the string makes an angle of $\frac{\pi}{3}$ with the ground. Determine an exact expression for the horizontal distance between the two positions of the kite along the ground.

